

Robotics I, WS 2024/2025

## Exercise Sheet 6

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Prof. Dr.-Ing. Tamim Asfour  
Adenauerring 12, Geb. 50.19  
Web: <https://www.humanoids.kit.edu/>

### Exercise 1

(Color representation)

1. Transform the following colors specified in the RGB model and into the HSI format.
  - i.)  (120, 80, 210)
  - ii.)  (0, 150, 130)
2. A robot observes at a pack of cereal in a windowless laboratory. Someone turns the light a little brighter.
  - i.) Do the R, G or B values of the cereal package change?
  - ii.) Do the H, S or I values of the cereal package change?
3. The robot observes the pack in a kitchen with windows. Outside, a cloud pushes in front of the sun.
  - i.) Do the R, G or B values of the cereal package change?
  - ii.) Do the H, S or I values of the cereal package change?

Exercise 2

(Camera Modell)

Given a pinhole camera in positive position with focal length  $f = 20mm$ :

1. You use it to photograph a building from a distance of 350 meters. In the picture, the building is  $0.8mm$  high. How high is the actual building?
2. You are taking a photo of Cologne Cathedral, which is known to be  $100\frac{\pi}{2}m$  high, from the opposite bank of the Rhine from a distance of  $800m$ . In your photo, the cathedral is 314 pixels high. How many pixels per millimeter does the camera have?

## Exercise 3

(Filters in Image Processing)

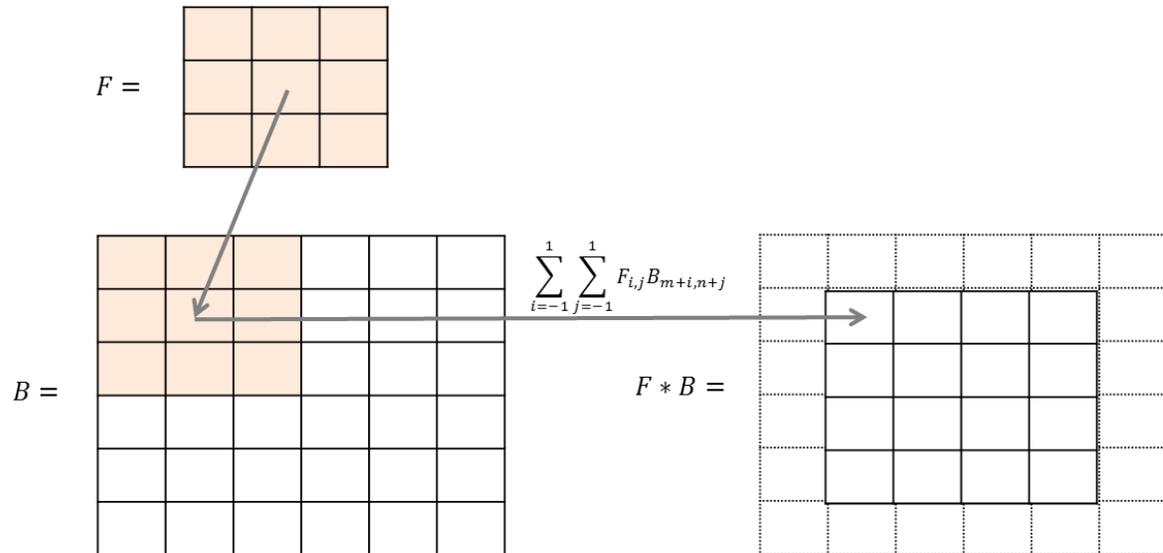


Figure 1: Filtering: 1) The filter matrix is placed over the original image. 2) Overlaying pixels are multiplied and the products are added. 3) The result forms the pixel value of the filtered image at the position of the filter. The edge pixels of the resulting image can be ignored in this task.

Given the following gray scale image  $B$ :

$$B = \begin{pmatrix} 20 & 20 & 20 & 20 & 40 & 40 & 40 & 40 & 30 & 30 & 30 \\ 20 & 20 & 20 & 20 & 40 & 40 & 40 & 40 & 30 & 30 & 30 \\ 20 & 20 & 20 & 20 & 40 & 40 & 40 & 40 & 30 & 30 & 30 \\ 50 & 50 & 50 & 50 & 50 & 50 & 50 & 50 & 20 & 20 & 20 \\ 20 & 50 & 50 & 50 & 50 & 50 & 50 & 50 & 20 & 20 & 20 \\ 20 & 20 & 50 & 50 & 50 & 50 & 50 & 50 & 20 & 20 & 20 \\ 20 & 20 & 20 & 50 & 50 & 50 & 50 & 50 & 20 & 20 & 20 \end{pmatrix}$$

1. Calculate the result of filtering  $B$  with a Prewitt-X Filter
2. Calculate the result of filtering  $B$  with a Prewitt-Y Filter

## Exercise 4

## Threshold Segmentation

1. In the image in Figure 2 an object should be detected. The image has already been converted to a greyscale image and the intensity values (0 ... 255) are denoted on the pixels. For segmentation, threshold segmentation is applied with a threshold of  $T = 51$ . Show the result of the segmentation by filling the pixels in Figure 2 (right).

|     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 255 | 212 | 74  | 181 | 176 | 176 | 196 | 171 | 156 | 255 | 212 | 74  | 181 | 176 | 176 | 196 | 171 | 156 |
| 181 | 219 | 23  | 135 | 163 | 56  | 46  | 69  | 56  | 181 | 219 | 23  | 135 | 163 | 56  | 46  | 69  | 56  |
| 186 | 148 | 79  | 186 | 230 | 163 | 64  | 54  | 84  | 186 | 148 | 79  | 186 | 230 | 163 | 64  | 54  | 84  |
| 166 | 237 | 69  | 179 | 166 | 69  | 120 | 112 | 245 | 166 | 237 | 69  | 179 | 166 | 69  | 120 | 112 | 245 |
| 43  | 194 | 194 | 179 | 107 | 117 | 99  | 87  | 43  | 43  | 194 | 194 | 179 | 107 | 117 | 99  | 87  | 43  |
| 222 | 5   | 186 | 163 | 115 | 77  | 105 | 46  | 71  | 222 | 5   | 186 | 163 | 115 | 77  | 105 | 46  | 71  |
| 207 | 186 | 10  | 13  | 41  | 43  | 43  | 54  | 201 | 207 | 186 | 10  | 13  | 41  | 48  | 43  | 54  | 201 |
| 189 | 196 | 89  | 64  | 128 | 71  | 89  | 74  | 54  | 189 | 196 | 89  | 64  | 128 | 71  | 89  | 74  | 54  |

Figure 2: Image which should be segmented (left). Use the right image to show the resulting segmentation.

2. How can the color information of the segmented object be preserved after segmentation.

## Exercise 5

(Iterative Closest Point (ICP))

The point cloud  $P = \{p_0, p_1, p_2\}$  shown in Figure 3 is to be registered with the triangle  $V = \{v_0, v_1, v_2\}$  using the *Iterative Closest Point (ICP)* algorithm.

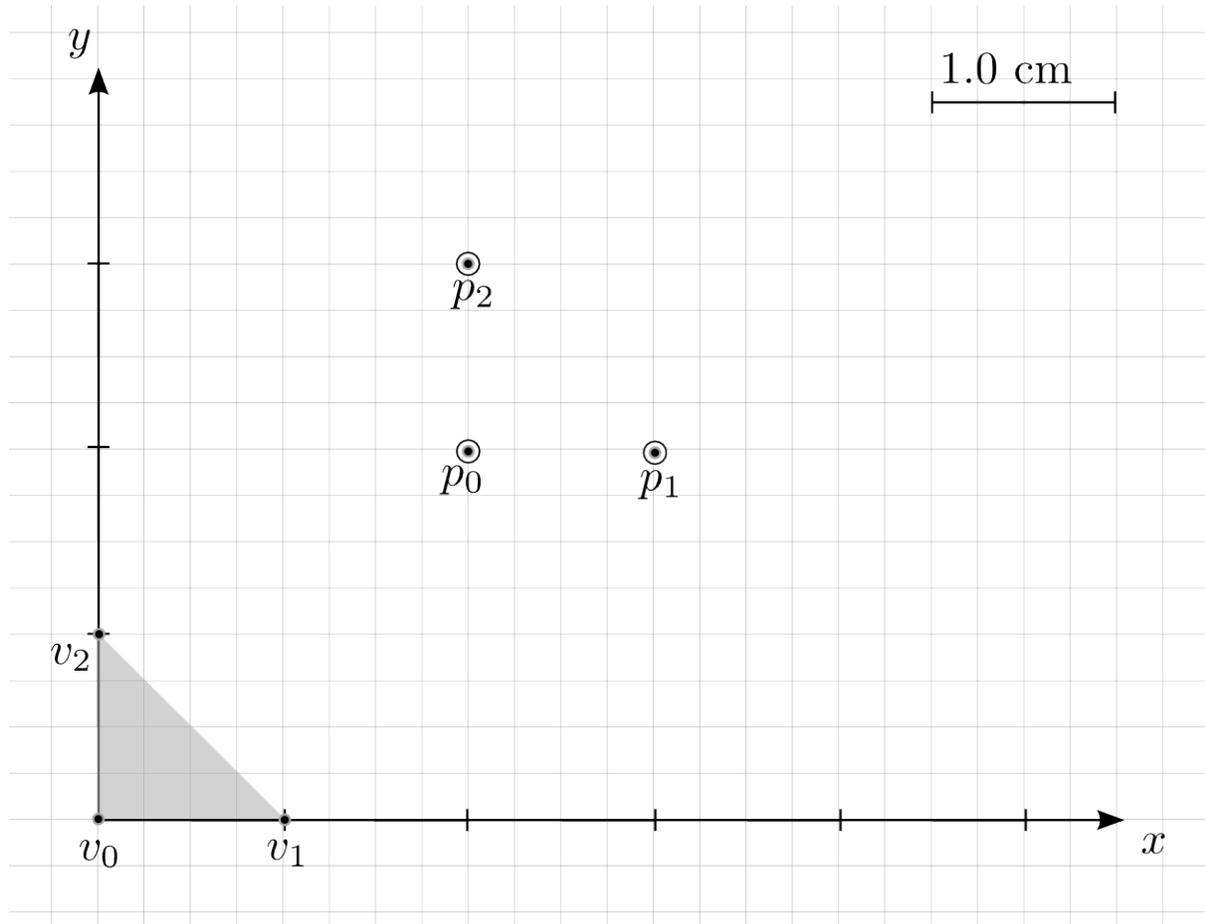


Figure 3: Point cloud  $P = \{p_0, p_1, p_2\}$  and triangle  $V = \{v_0, v_1, v_2\}$

1. Setup the error function  $F_T$  for the ICP-algorithm
2. To solve the problem the ICP-algorithm is to be applied using the steepest gradient approach. Determine the simplified error function.

$$F_T' = (\|v_0 - p_0\|)^2.$$

3. For the ICP algorithm from the second part of the task, specify the function that approximates  $V$  to  $P$  with a step size  $\alpha$ . Draw the first two iterations for  $\alpha = 0.25$  in Figure 3.